

|              |   |
|--------------|---|
| $P_s$        | vapor pressure  |
| $q$          | pure-component area parameter                         |
| $r$          | pure-component volume parameter                       |
| $R$          | gas constant  |
| $T$          | temperature in Kelvin degrees                         |
| $x$          | mole fraction in the liquid phase                     |
| $y$          | mole fraction in the vapor phase                      |
| $ \Delta y $ | absolute average deviation of vapor-phase composition |
| $z$          | coordination number                                   |

#### Greek Letters

|          |                               |
|----------|-------------------------------|
| $\gamma$ | activity coefficient          |
| $\phi$   | segment fraction              |
| $\Delta$ | parameter of Wilson equation  |
| $\sigma$ | mean standard deviation       |
| $\tau$   | parameter of UNIQUAC equation |
| $\theta$ | area fraction                 |

#### Subscripts

|   |              |
|---|--------------|
| 1 | hydrocarbons |
| 2 | nitriles     |

|       |  |
|-------|--|
| $i$   | index                                  |
| exptl | experimental values                    |
| calcd | calculated values                      |
| W     | value calculated with Wilson equation  |
| U     | value calculated with UNIQUAC equation |

#### Exponent

|          |                   |
|----------|-------------------|
| $\infty$ | infinite dilution |
|----------|-------------------|

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## Density, Viscosity, and Surface Tension of Mixed Molten Hydrates. 2. Mixtures of Zinc Nitrate and Nickel Nitrate Hexahydrates

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Densities, viscosities, and surface tensions of mixtures containing  $Zn(NO_3)_2 \cdot 6H_2O$  and  $Ni(NO_3)_2 \cdot 6H_2O$  have been measured as a function of temperature and composition. The equivalent volume-composition and fluidity-composition isotherms were linear but the surface tension-composition isotherms exhibited appreciable negative deviations from the additive values, the deviations being the maximum around equimolar composition. The fluidity data were fitted to the equations  $\phi = A_\phi T^{-1/2} \exp[-B_\phi / (T - T_{0,\phi})]$  and  $\phi = A_\phi' \exp[-B_\phi' / (V - V_{0,\phi})]$  based upon the free volume model;  $A_\phi$ ,  $B_\phi$ ,  $T_{0,\phi}$ ,  $A_\phi'$ ,  $B_\phi'$ , and  $V_{0,\phi}$  are empirical parameters. Composition dependences of these parameters have been discussed.

### Introduction

Recently, quite a few reports concerning the physicochemical studies of hydrated melts in pure and mixed states have been published (3, 14, 16-19). Moynihan et al. (21) has shown that the system containing the molten tetrahydrates of calcium and cadmium nitrates behaves nearly ideal above 60 °C but considerable negative deviations in conductance and fluidity isotherms are observed at lower temperatures. A nonideal character of mixing the molten hydrates is also apparent from the studies of the system  $Cr(NO_3)_3 \cdot 9H_2O + (Ca, Cd)(NO_3)_2 \cdot 4H_2O$  (19).

In order to examine whether such nonideal behavior is related to the polarizability, charge type, and/or the nature of the hydration sphere of the two constituent cations, we selected the present system containing the cations of the same charge to

radius ratio and having a similar hydration sphere. The present paper thus presents some of the observations on the system containing the molten hydrates of zinc and nickel nitrate hexahydrate.

### Experimental Section

Hexahydrates of nickel nitrate (BDH) and zinc nitrate (S. Merck) were of LR grade purity. The melting temperatures of these salts as determined by the cooling curve method were 56.8 and 36.8 °C for the nickel and zinc salt, respectively, with corresponding literature (26) values being 56.7 and 37 °C. An agreement between the measured melting temperatures and the literature melting temperatures leads one to believe that the salts were of the stoichiometry as given by the manufacturers. This was verified for zinc nitrate hexahydrate by an EDTA titration (24) and for nickel nitrate hexahydrate by a gravimetric (24) method by precipitating  $Ni^{2+}$  as dimethylglyoxime. Repeated cross checks gave the water content to be within  $\pm 0.02$  of the stoichiometric value of six.

Mixtures were prepared by melting the requisite amounts of the salts in Pyrex glass flasks (ca. 100 cm<sup>3</sup>) fitted with a airtight ground glass joint at the top and filtered in situ through glass filters (porosity G-3) under a slight positive pressure of dry, CO<sub>2</sub>-free air. Filtered melts were then maintained at about 60-70 °C for about 1 h, for maturing.

Densities were measured by measuring the volumes of a certain amount of melt in a precalibrated densitometer capable of reading up to 0.01 cm<sup>3</sup>. The details regarding the design and calibration of the densitometer and the measuring technique have been described earlier (16, 17). Estimated accuracy of experimental densities is  $\pm 0.1\%$ .

Table I. Density/Equivalent Volume-Temperature Equations for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  Mixtures

| mol %<br>$\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ | temp<br>range, K | no. of<br>data<br>points | $\rho$ ( $\text{g cm}^{-3}$ ) = $a - b(T - 273.15)$ |          |                    |                    | $V_e$ ( $\text{cm}^3 \text{equiv}^{-1}$ ) = $A + B(T - 273.15)$ |          |       |        | $10^4 \alpha$<br>(348 K),<br>$\text{deg}^{-1}$ |
|---|------------------|--------------------------|---|----------|--------------------|--------------------|---|----------|-------|--------|--|
|   |                  |                          | $a$   | $10^3 b$ | $10^3 \text{SE}^b$ | $10^3 \text{MD}^c$ | $A$   | $10^2 B$ | SE    | MD     |  |
| 0.0 <sup>a</sup>  | 312-353          | 7                        | 1.8707  | 1.154    | 0.15               | 0.25               | 79.39   | 5.29     | 0.012 | -0.015 | 6.27   |
| 9.70  | 303-349          | 8                        | 1.8654  | 1.215    | 0.25               | 0.41               | 79.47   | 5.56     | 0.018 | -0.026 | 6.66   |
| 22.45   | 307-347          | 7                        | 1.8701  | 1.188    | 0.33               | 0.50               | 79.04   | 5.40     | 0.020 | +0.028 | 6.49   |
| 27.97   | 309-349          | 8                        | 1.8719  | 1.169    | 0.12               | -0.18              | 78.86   | 5.30     | 0.008 | -0.01  | 6.40   |
| 38.92   | 310-348          | 7                        | 1.8688  | 1.153    | 0.20               | 0.36               | 78.80   | 5.22     | 0.013 | -0.021 | 6.32   |
| 50.53   | 310-350          | 8                        | 1.8684  | 1.087    | 0.27               | -0.39              | 78.62   | 4.90     | 0.013 | -0.017 | 5.95   |
| 58.79   | 320-352          | 6                        | 1.8721  | 1.124    | 0.24               | 0.34               | 78.28   | 5.09     | 0.014 | -0.020 | 6.19   |
| 70.48   | 312-351          | 7                        | 1.8727  | 1.088    | 0.26               | -0.36              | 78.08   | 4.87     | 0.016 | +0.022 | 5.96   |
| 79.00   | 321-349          | 6                        | 1.8725  | 1.050    | 0.07               | -0.12              | 77.93   | 4.70     | 0.005 | -0.007 | 5.77   |
| 91.19   | 319-349          | 6                        | 1.8731  | 1.020    | 0.15               | 0.20               | 77.69   | 4.54     | 0.008 | -0.009 | 5.60   |
| 100.00  | 322-349          | 6                        | 1.8709  | 0.963    | 0.21               | -0.22              | 77.63   | 4.28     | 0.011 | -0.011 | 5.29   |

<sup>a</sup> Adopted from ref 18. <sup>b</sup> SE = standard error. <sup>c</sup> MD = mean deviation.

Table II. Surface Tension ( $\sigma$ ) and Related Parameters of  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  Mixtures

| mol %<br>$\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ | temp range, K | $\sigma$ ( $\text{mN m}^{-1}$ ) = $a - bT$ (K) |        |               | $10^2 (H^\sigma/A^\sigma)$ ,<br>$\text{J m}^{-2}$ | $10^4 (S^\sigma/A^\sigma)$ ,<br>$\text{J m}^{-2} \text{K}^{-1}$ |
|---|---------------|--|--------|---------------|---|---|
|   |               | $a$  | $b$    | $\text{SE}^a$ |   |   |
| 0.0   | 312-350       | 128.83   | 0.111  | 0.27          | 12.88   | 1.11  |
| 9.7   | 313-347       | 144.44   | 0.1576 | 0.012         | 14.44   | 1.58  |
| 22.4  | 313-349       | 134.73   | 0.1351 | 0.046         | 13.47   | 1.35  |
| 28.0  | 314-348       | 135.13   | 0.1384 | 0.019         | 13.51   | 1.38  |
| 38.9  | 314-350       | 128.26   | 0.1235 | 0.250         | 12.83   | 1.23  |
| 50.5  | 315-352       | 122.30   | 0.1100 | 0.129         | 12.23   | 1.10  |
| 58.8  | 323-351       | 124.32   | 0.1040 | 0.084         | 12.43   | 1.04  |
| 70.5  | 320-349       | 124.37   | 0.1017 | 0.013         | 12.44   | 1.02  |
| 79.0  | 331-349       | 123.38   | 0.0928 | 0.087         | 12.34   | 0.93  |
| 91.2  | 331-349       | 125.62   | 0.0968 | 0.070         | 12.56   | 0.97  |
| 100.0   | 323-350       | 136.22   | 0.1260 | 0.002         | 13.62   | 1.26  |

<sup>a</sup> SE = standard error.

Viscosities were measured with Cannon-Fenske type viscometers, calibrated with aqueous solutions of sucrose and glycerol (18); the viscometer constants were 0.2009 and 0.2647  $\text{cP s}^{-1}$ . Inherent accuracy of these measurements is estimated to be  $\pm 0.5\%$ .

Surface tensions were measured by the differential capillary rise method described in detail earlier (18). Under the conditions of thermal equilibrium, the temperature did not vary by more than  $\pm 0.1^\circ\text{C}$  over the region of interest. The difference in the levels of the liquid in the two capillaries was measured with a precision of  $\pm 0.001$  cm. Measured surface tensions are estimated to be accurate to  $\pm 0.3\%$ . In all measurements the temperatures were controlled and measured with a precision of  $\pm 0.1^\circ\text{C}$ .

## Results and Discussion

**Densities and Equivalent Volumes.** The density results for various mixtures of the  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  system were expressed in the form of linear density ( $\rho$ )-temperature and equivalent volume ( $V_e$ )-temperature equations and are presented in Table I. The maximum departure of any experimental point from the least-squares straight line and the expansivity ( $\alpha = (1/V_e)(dV_e/dT)$ ) for each composition are also included in Table I. A typical equivalent volume-composition (mole percent of nickel nitrate hexahydrate) isotherm at  $75^\circ\text{C}$  is shown in Figure 1. The volumes are found to be additive over the entire composition range. The extrapolated value for the equivalent volume of  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  at  $75^\circ\text{C}$ , estimated from the present data, is  $83.75 \text{ cm}^3 \text{equiv}^{-1}$ . This can be very favorably compared to the value  $83.36 \text{ cm}^3 \text{equiv}^{-1}$  obtained from the direct measurements (18).

**Surface Tension.** For all mixtures, surface tension ( $\sigma$ ) varied linearly with temperature. These  $\sigma$ - $T$  equations are presented in Table II. The surface tensions and their temperature coefficients are comparable to that for aqueous solutions of electrolytes. This leads to the belief that the surface tension

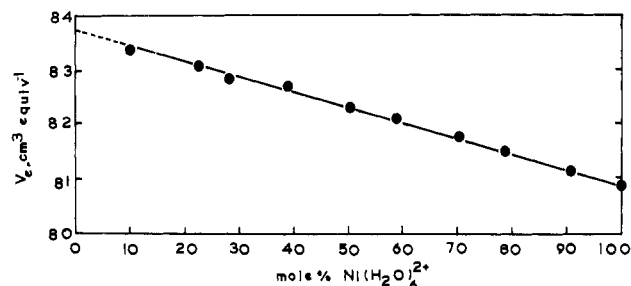


Figure 1. Variation of equivalent volume of  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  mixtures with mole percent of  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  at  $75^\circ\text{C}$ .

of these liquids is governed by the electrostricted dipoles of water.

The surface tension of a liquid is defined (9) as its surface free energy per unit area, i.e.

$$\sigma = G^\sigma/A^\sigma \quad (1)$$

where  $A^\sigma$  is the area of the surface. The surface entropy per unit area ( $S^\sigma/A^\sigma$ ) and the surface enthalpy per unit area ( $H^\sigma/A^\sigma$ ) are then described as

$$S^\sigma/A^\sigma = -d\sigma/dT \quad (2)$$

$$H^\sigma/A^\sigma = \sigma - T(d\sigma/dT) \quad (3)$$

As the temperature coefficient of surface tension for these mixtures is constant, the  $H^\sigma/A^\sigma$  is a constant and independent of temperature. Table II lists the values of  $H^\sigma/A^\sigma$  and  $S^\sigma/A^\sigma$  for all the mixtures investigated in this study. The magnitude of  $H^\sigma/A^\sigma$  appears to place these molten hydrates between highly ionized molten salts and the nonpolar liquids; the magnitude for this parameter usually lies around  $0.2 \text{ J m}^{-2}$  for the former and  $0.05 \text{ J m}^{-2}$  for the latter class of liquids. The variation of surface tension at  $350 \text{ K}$  with the mole percent of  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  is shown in Figure 2. The negative deviations and the occurrence

Table III. Parameters for the Least-Square Fit of the Fluidity-Temperature Data of  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  Mixtures

| mol %<br>$\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ | temp<br>range, K | no. of<br>data<br>points | $\phi$ ( $\text{cP}^{-1}$ ) = $A_\phi T^{-1/2} \exp[-B_\phi/(T - T_{0,\phi})]$ |          |              |                    | $\phi$ ( $\text{cP}^{-1}$ ) = $A_\phi' T^{-1/2} \exp[-675/(T - T_{0,\phi})]$ |              |                    | $T_g, ^\circ\text{C}$ K |     |
|---|------------------|--------------------------|--|----------|--------------|--------------------|--|--------------|--------------------|-------------------------|-----|
|   |                  |                          | $A_\phi$   | $B_\phi$ | $T_{0,\phi}$ | $10^3 \text{SE}^b$ | $A_\phi'$  | $T_{0,\phi}$ | $10^3 \text{SE}^b$ |                         |     |
| 0.0 <sup>a</sup>  | 302-353          | 9                        | 142.58   | 638.43   | 183.60       | 0.44               | 161.99   | 179.66       | 0.54               | 197                     |     |
| 9.7   | 303-349          | 8                        | 117.98   | 593.92   | 188.98       | 0.46               | 157.72   | 180.16       | 0.64               |                         |     |
| 22.4  | 307-347          | 7                        | 152.16   | 682.55   | 181.43       | 0.12               | 148.23   | 182.22       | 0.12               |                         |     |
| 28.0  | 305-349          | 8                        | 151.05   | 689.95   | 181.00       | 0.24               | 143.41   | 182.56       | 0.23               |                         |     |
| 38.9  | 310-348          | 7                        | 130.30   | 659.05   | 185.97       | 0.13               | 137.78   | 184.27       | 0.12               |                         |     |
| 50.5  | 310-350          | 8                        | 169.33   | 782.29   | 172.82       | 0.18               | 118.36   | 183.78       | 0.19               |                         |     |
| 58.8  | 311-352          | 8                        | 149.74   | 746.39   | 178.97       | 0.18               | 117.38   | 186.28       | 0.19               |                         |     |
| 70.5  | 316-351          | 8                        | 84.50  | 607.74   | 194.32       | 0.32               | 107.13   | 186.94       | 0.33               |                         |     |
| 79.0  | 320-349          | 6                        | 94.75  | 675.07   | 188.34       | 0.10               | 94.72  | 188.34       | 0.10               |                         |     |
| 91.2  | 319-349          | 6                        | 74.79  | 639.93   | 194.58       | 0.15               | 84.72  | 190.85       | 0.16               |                         |     |
| 100.0   | 327-355          | 5                        | 1957.03  | 1950.07  | 91.23        | 0.31               | 78.58  | 193.72       | 0.53               |                         | 210 |

<sup>a</sup> Adopted from ref 18. <sup>b</sup> SE = standard error. <sup>c</sup> Estimated from ref 8.

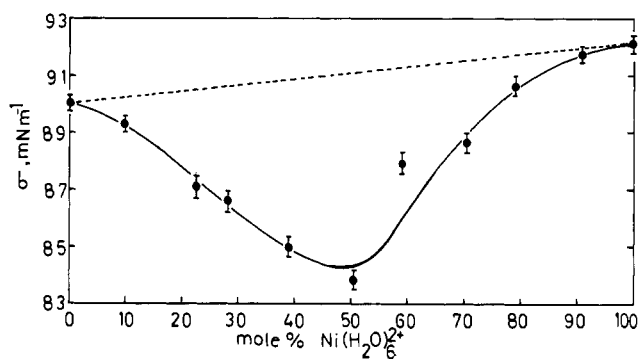


Figure 2. Variation of surface tension ( $\sigma$ ) (at 350 K) for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  mixtures, with mole percent of nickel nitrate hexahydrate.

of minima around 50 mol % of the nickel salt give this plot a considerable significance. Apparently similar isotherms have also been observed (19) for  $\text{Cr}(\text{NO}_3)_3 \cdot 9\text{H}_2\text{O} + (\text{Ca}, \text{Cd})(\text{NO}_3)_2 \cdot 4\text{H}_2\text{O}$  systems, where the minima are observed around 30 mol % of divalent ion hydrate. These results when taken together indicate that the position of the minima in  $\sigma$ -composition isotherms may be a reflection of either the nature of the hydration sphere or charge type of the component cations of the system. According to Bloom et al. (9), the deviations in surface tension values from ideal behavior values can be explained in terms of surface enthalpy and surface entropy of mixing per unit area, given by

$$\Delta(H^\sigma/A^\sigma) = (H^\sigma/A^\sigma) - \{X_1(H^\sigma/A^\sigma)_1 + X_2(H^\sigma/A^\sigma)_2\} \quad (4)$$

$$\Delta(S^\sigma/A^\sigma) = (S^\sigma/A^\sigma) - \{X_1(S^\sigma/A^\sigma)_1 + X_2(S^\sigma/A^\sigma)_2\} \quad (5)$$

where  $(H^\sigma/A^\sigma)$  and  $(S^\sigma/A^\sigma)$  are the surface enthalpy and surface entropy per unit area for the mixture and the quantities with the subscript 1 and 2 refer to those of pure components; these were evaluated through relations 2 and 3. The variation of  $\Delta(H^\sigma/A^\sigma)$  and  $\Delta(S^\sigma/A^\sigma)$  values with the composition of the mixture is presented in Figure 3. The small positive surface enthalpy and entropy of mixing per unit area for solutions rich in zinc nitrate could be due to a loosening of the cation-water dipole bonding, resulting because of competition between water and  $\text{NO}_3^-$  for occupying a site next to the cation. Negative values of  $\Delta(H^\sigma/A^\sigma)$  and  $\Delta(S^\sigma/A^\sigma)$  for melts richer in nickel nitrate hexahydrate can then be considered a reflection of some ordering tendencies resulting from the difference in the strength of ion-dipole interactions for the two cations.

**Fluidity.** The variation of fluidity of the system  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  with the composition at 75 °C is shown in Figure 4. The system behaves ideally with respect to flow characteristics. The  $\ln \phi$  vs.  $T^{-1}$  plots (not given) showed slight curvature in a direction corresponding to an increase in the

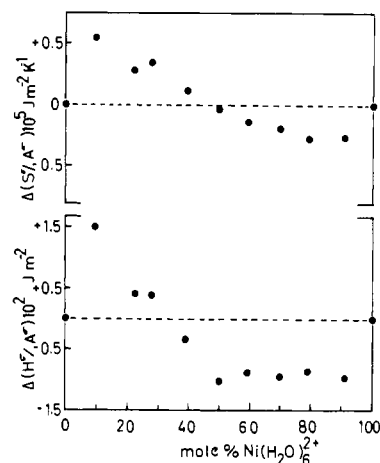


Figure 3. Variation of surface enthalpy and surface entropy of mixing per unit area, with composition (mol %  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ ) for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  mixtures.

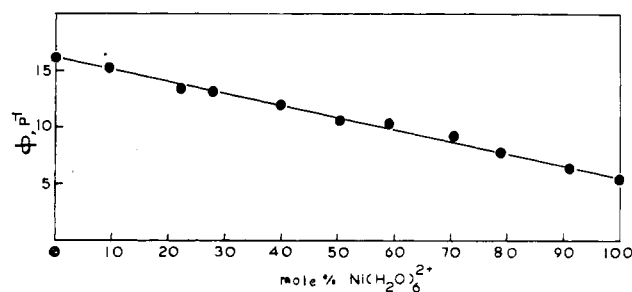


Figure 4. Fluidity (at 75 °C) vs. mole percent of  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  plot for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  mixtures.

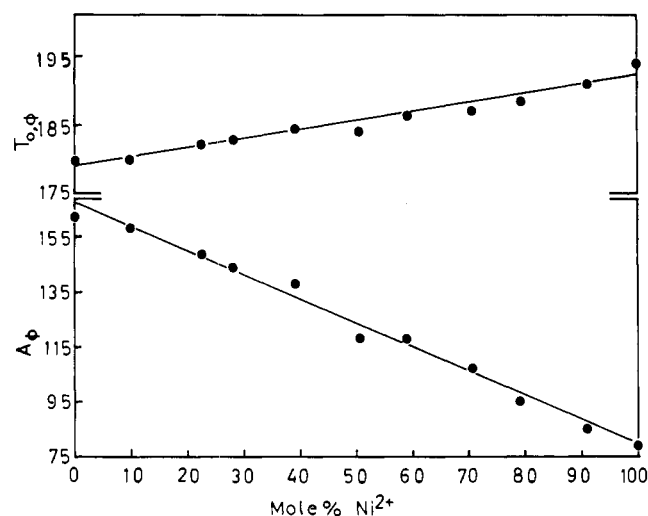
apparent activation energy with decreasing temperatures. Such non-Arrhenius behavior exhibited by concentrated electrolyte solutions in the fluidity range of  $10^{-1}$ – $10$   $\text{P}^{-1}$  has frequently been interpreted in terms of the Vogel-Tammann-Fulcher (12, 23, 25) equation

$$\phi = A_\phi T^{-1/2} \exp[-B_\phi/(T - T_{0,\phi})] \quad (6)$$

where,  $A_\phi$ ,  $B_\phi$ , and  $T_{0,\phi}$  are constants. The parameter  $T_{0,\phi}$  has been interpreted as the zero mobility temperature at which free volume (10) or the configurational entropy (1) becomes zero. The fluidity data obtained in this study were processed on a IBM 360/44 data processing system to fit into eq 6 by an iterative method. Refinement in the values of the parameters  $A_\phi$ ,  $B_\phi$ , and  $T_{0,\phi}$  were carried out till the two successive values of these parameters did not differ by more than  $\pm 0.01$ . In Table III are recorded the parameters  $A_\phi$ ,  $B_\phi$ , and  $T_{0,\phi}$  obtained from the least-squares fit of the fluidity data. Inspection of the best fit parameters does not reveal any systematic trends in  $A_\phi$ ,  $B_\phi$ ,

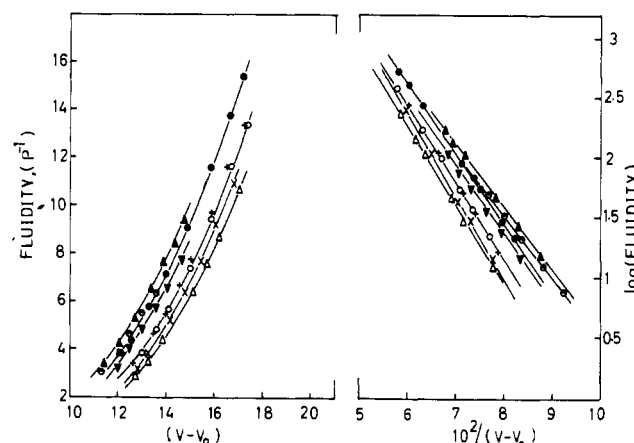
Table IV. Least-Square Fits of the Fluidity-Molar Volume Data for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  Mixtures

| mol %<br>$\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ | temp range, K | $\phi (\text{P}^{-1}) = A_\phi' \exp[-B_\phi'/(V - V_{0,\phi})]$ |  |   |                    |        | $V_{0,\text{extrap}}$ ,<br>$\text{cm}^3 \text{mol}^{-1}$ | $\gamma$ |
|---|---------------|--|--|---|--------------------|--------|--|----------|
|   |               | $A_\phi'$ ,<br>$\text{P}^{-1}$                                   | $B_\phi'$ ,<br>$\text{cm}^3 \text{mol}^{-1}$ | $V_{0,\phi}$ ,<br>$\text{cm}^3 \text{mol}^{-1}$ | $10^2 \text{SE}^a$ |        |  |          |
| 0.0   | 302-353       | 540.70   | 59.56  | 149.85  | 0.37               | 148.93 | 0.397  |          |
| 9.7   | 303-349       | 454.35   | 58.30  | 150.14  | 0.44               | 148.62 | 0.389  |          |
| 22.4  | 307-347       | 571.38   | 65.11  | 148.75  | 0.17               | 148.28 | 0.438  |          |
| 28.0  | 305-349       | 567.58   | 64.69  | 148.52  | 0.22               | 148.14 | 0.436  |          |
| 38.9  | 310-348       | 491.78   | 60.91  | 149.03  | 0.16               | 148.34 | 0.408  |          |
| 50.5  | 310-350       | 620.33   | 67.83  | 147.95  | 0.37               | 148.50 | 0.459  |          |
| 58.8  | 311-352       | 553.13   | 67.36  | 147.53  | 0.31               | 147.74 | 0.456  |          |
| 70.5  | 316-351       | 320.92   | 52.20  | 148.93  | 0.66               | 147.78 | 0.352  |          |
| 79.0  | 320-349       | 353.92   | 56.15  | 148.37  | 0.19               | 147.90 | 0.378  |          |
| 91.2  | 319-349       | 284.22   | 51.60  | 148.69  | 0.29               | 147.92 | 0.347  |          |
| 100.0   | 327-355       | 5608.34  | 188.67                                       | 136.39  | 0.61               | 148.48 |  |          |

<sup>a</sup> SE = standard error.Figure 5. Variations of parameters  $A_\phi$  and  $T_{0,\phi}$  (eq 6) with mol % of  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  mixtures.

and  $T_{0,\phi}$  values. This might be a reflection of a strong interdependence of these parameters, so that if the data do not cover a reasonably extensive range in the magnitude of fluidity values, the system can be described equally well by a number of different  $A_\phi - B_\phi - T_{0,\phi}$  sets. To investigate if there existed any significant composition dependence of  $A_\phi$  and  $T_{0,\phi}$ , we assumed that the value of  $B_\phi$ , the exponential coefficient in eq 6, is independent of composition as observed for a large variety of fused nitrates and chlorides (2-6, 20). The fluidity data were processed to fit eq 6 at a constant value of 675 K for  $B_\phi$  (cf. Moynihan et al. (21) and Jain (19)) without much loss of precision of the fit. The computed parameters are presented in Table III. The estimated  $T_{0,\phi}$  values for pure salts lie about 16-17 °C below the experimentally determined glass transition temperatures (8). Lower  $T_0$  (or  $T_g$ ) values for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  relative to  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  and a systematic variation of  $T_{0,\phi}$  with the composition of the melt (Figure 5) across the composition range could be rationalized (7) in terms of  $m^{-1/2}$  dependence of  $T_g$  (hence  $T_0$ ) on the effective masses of the component particles of the amorphous phase and also  $r^{-1}$  dependence of  $T_0$  (hence  $T_g$ ) on cation radii. Rao et al. (22), however, ascribed this lowering in  $T_0$  values to the presence of more covalent character in metal-nitrate ion bonding in the case of more polarizable cations, it being  $\text{Zn}^{2+}$  in this case.

The values of the preexponential coefficient,  $A_\phi$ , systematically decrease (Figure 5) in going from zinc nitrate to nickel nitrate hexahydrate, indicating a direct dependence of  $A_\phi$ 's on the cationic mass, a trend in the reverse direction to that predicted by the theory (10). Similar observations, have also been made by Moynihan et al. (21) and Jain (19). The interesting

Figure 6. Fluidity vs.  $(V - V_{0,\phi})$  and  $\log(\text{fluidity})$  vs.  $(V - V_{0,\phi})^{-1}$  plots for  $\text{Zn}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O} + \text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$  mixtures: (●) 9.7, (○) 22.4, (+) 28.0, (×) 50.5, (Δ) 58.8, (▲) 70.5, (▼) 79.0, and (⊙) 91.2 mol % of  $\text{Ni}(\text{NO}_3)_2 \cdot 6\text{H}_2\text{O}$ .

observation at this stage is that the preexponential factor,  $A_\phi$ , goes almost parallel to the thermal expansivity ( $\alpha$ ) of the medium, thereby indicating that the parameter  $A_\phi$  is related to the rigidity of the medium.

The discrepancy between theory and the experiment has also been explained (21) by postulating that the composition dependence of  $A_\phi$ 's may be related to the differences in the lability of the water or nitrate ion in the coordination shell of the cations.

Doolittle (11) and Williams, Landel, and Ferry (27) have empirically shown that the viscosity can be related to the free volume in a liquid, by the relation

$$\eta = A \exp(BV_0/V_f) \quad (7)$$

where  $V_f$  is the free volume and  $V_0$  the closed packed molecular volume and  $A$  and  $B$  are the constants. Cohen and Turnbull (10) placed this expression on a solid theoretical basis by deriving eq 7 under the considerations of "hard-sphere" model for liquids. Recently, Doolittle's equation in the form

$$\phi = A_\phi' \exp[-B_\phi'/(V - V_{0,\phi})] \quad (8)$$

was found to hold good for describing the temperature dependence of transport properties of certain glass-forming anhydrous (15) and hydrated melts (14, 19), the terms  $A_\phi'$  and  $B_\phi'$  being empirical parameters,  $V$  the volume per mole of the salt at any temperature, and  $V_{0,\phi}$  the intrinsic volume, i.e., the molar volume at  $T_{0,\phi}$ . Hildebrand (13) proposed the equation

$$\phi = B(V - V_0)/V_0 \quad (9)$$

to describe the dependence of fluidity on the free volume in the liquid. Plots of fluidity vs.  $(V - V_0)$  tend to be nonlinear (Figure 6) indicating the inadequacy of the Hildebrand equation for de-

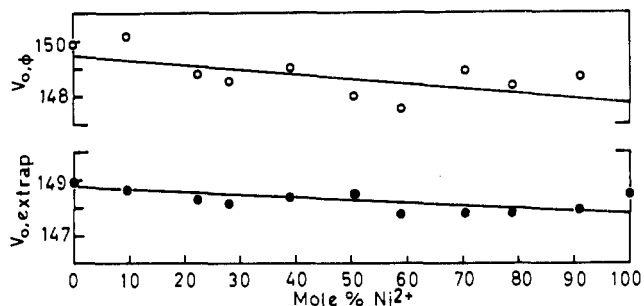


Figure 7. The variation of intrinsic volume,  $V_{0,\phi}$  (O), and the molar volume at  $T_0$  (K),  $V_{0,extrap}$  (●), for  $Zn(NO_3)_2 \cdot 6H_2O + Ni(NO_3)_2 \cdot 6H_2O$  mixtures, with the mole percent of nickel nitrate hexahydrate.

describing the dependence of fluidity on the free volume for the system investigated in this study. To test the relevance of the Doolittle equation, we fitted the present fluidity data into eq 8 by an *iterative* method as described above. The "best fit" parameters are listed in Table IV. Linear plots obtained when  $\ln \phi$  is plotted against  $(V - V_{0,\phi})^{-1}$  (Figure 6) demonstrate the success of eq 8 in describing the free volume dependence of fluidity in the systems investigated presently.  $V_{0,\phi}$  is shown as a function of composition in Figure 7. It is interesting to note that the  $V_0$ 's obtained by extrapolating the equations

$$V = \alpha + \beta(T - 273.15) \quad (10)$$

to  $T_{0,\phi}$  (K) are nearly equal to those obtained from the least-squares fit of the fluidity-molar volume data. This recognizes the view that free volume becomes zero at  $T_{0,\phi}$  (K) and not 0 K. A poorer agreement between  $V_{0,\phi}$  and  $V_{0,extrap}$  for  $Ni(NO_3)_2 \cdot 6H_2O$  may be due to the smaller temperature range of investigation for this salt. The parameters  $V_{0,\phi}$  and  $V_{0,extrap}$  may be considered to vary linearly ( $\pm 1\%$ ) with composition. The interesting fact which emerges out from this analysis is that  $V_0$ 's for the two salts are nearly equal, despite a sizable difference in their isothermal molar volumes. This appears to be a direct reflection of the differences in the  $\alpha$  values and the temperature

range ( $= T - T_{0,\phi}$ ) over which the extrapolation is made.

The exponential coefficient ( $B_\phi'$ ), according to the "hard sphere" model (10) equals the product  $\gamma V_{0,\phi}$ ,  $\gamma$  being a geometric factor to correct for the overlap of free volume in the calculation of probability of occurrence of a critical void. The computed values of  $\gamma$  (0.34–0.46) are considerably lower than the value 0.5–1 required by theory (10). This indicates that a random distribution of free volume is apparently not obtained in these systems.

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